



## I B.TECH I Sem Supplementary Examination, December 2021

**MATHEMATICS - I**  
**(CE, CSE, ECE, EEE, IT, MECH)**
**Time: 3 Hours.****Max. Marks: 70**

Note: 1. Question paper consists: Part-A and Part-B.

2. In Part - A, answer all questions which carries 20 marks.

3. In Part - B, answer any one question from each unit.

Each question carries 10 marks and may have a, b as sub questions.

**PART- A****(10\*2 Marks = 20 Marks)**

- |       |  |    |     |     |
|-------|--|----|-----|-----|
| 1. a) | Define the rank of a matrix.   | 2M | CO1 | BL1 |
| b)    | Explain the reduction of normal form.  | 2M | CO1 | BL4 |
| c)    | Prove that the matrices A and its transpose have the same Eigen values                 | 2M | CO2 | BL3 |
| d)    | State Cayley-Hamilton theorem  | 2M | CO2 | BL1 |
| e)    | State D-Alembert's ratio test  | 2M | CO3 | BL1 |
| f)    | Define absolute and conditional converges of an infinite series                        | 2M | CO3 | BL1 |
| g)    | Explain the geometrical representation of Rolle's mean value theorem.                  | 2M | CO4 | BL4 |
| h)    | Define the Gamma function.   | 2M | CO4 | BL1 |
| i)    | State Euler's Theorem.   | 2M | CO5 | BL1 |
| j)    | Write the working rule to find the maximum and minimum values of the function $f(x,y)$ | 2M | CO5 | BL2 |

**PART- B****(10\*5 Marks = 50 Marks)**

- 2 a) Apply Gauss-Seidel iteration method to solve the following equations  
 $20x + y - 2z = 17$ ,  $3x + 20y - z = -18$ ,  $2x - 3y + 20z = 25$ 
10M CO1 BL3

**OR**

- 3 Investigate the values of  $\lambda$  and  $\mu$  so that the following equations  
 $2x + 3y + 5z = 9$ ,  $7x + 3y - 2z = 8$ ,  $2x + 3y + \lambda z = \mu$ , have (i) no solutions, (ii) a unique solutions, and (iii) an infinite number of solutions
10M CO1 BL4

- 4 a) Find the Eigen values and Eigen vectors of the matrix following matrix,
- $$A = \begin{bmatrix} 2 & 3 & 4 \\ 0 & 4 & 2 \\ 0 & 0 & 3 \end{bmatrix}$$
- 5M CO2 BL3

b) Using Cayley-Hamilton theorem, find the inverse of  $A = \begin{bmatrix} 3 & 2 & 4 \\ 4 & 3 & 2 \\ 2 & 4 & 3 \end{bmatrix}$ . 5M C02 BL3

**OR**

5 Reduce the quadratic form  $2xy + 2xz - 2yz$  to canonical form. 10M C02 BL4

Test the convergence of the series

6  $\frac{1}{2} + \frac{2}{3}x + \left(\frac{3}{4}\right)^2 x^2 + \left(\frac{4}{3}\right)^3 x^3 + \dots \infty (x > 0)$ . 10M C03 BL5

**OR**

7 Determine the nature of the series  $\sum_{n=2}^{\infty} \frac{1}{n(\log n)^p} (p > 0)$ . 10M C03 BL3

8 Prove that (if  $0 < a < b < 1$ ),  $\frac{b-a}{1+b^2} < \tan^{-1} b - \tan^{-1} a < \frac{b-a}{1+a^2}$ . Hence show that  $\frac{\pi}{4} + \frac{3}{25} < \tan^{-1} \frac{4}{3} < \frac{\pi}{4} + \frac{1}{6}$ . 10M C04 BL3

**OR**

9 State and prove the relationship between Beta and Gamma Functions. 10M C04 BL4

10 If  $u = (x^2 + y^2 + z^2)^{-1/2}$ , then prove that  $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \frac{\partial^2 u}{\partial z^2} = 0$ . 10M C05 BL3

**OR**

11 A rectangular box open at the top is to have volume of 32 cubic feet. Find the dimensions of the box requiring least material for its construction. 10M C05 BL4

---oo0oo---