



I B.Tech II Sem Supply Examination, March 2021

MATHEMATICS-II**(CIVIL, EEE, MECH, ECE, CSE & IT)****Time: 3 Hours.****Max. Marks: 70**

Note: 1. Answer any FIVE questions.

2. Each question carries 14 marks and may have a, b as sub questions.

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| 1 | a) | Solve the differential equation $\frac{dy}{dx} + \frac{2}{x}y = x^2y^2$. | 7M | C01 | R |
| | b) | Solve: $(x^2 - ay)dx = (ax - y^2)dy$. | 7M | C01 | U |
| 2 | a) | A body originally at $80^\circ C$ cools down to $60^\circ C$ in 20 minutes, the temperature of the air being $40^\circ C$. What will be the temperature of the body after 40 minutes from the original? | 7M | C01 | Ap |
| | b) | Solve: $(y - px)(p - 1) = p$ | 7M | C01 | U |
| 3 | a) | Solve: $\frac{d^2y}{dx^2} + 4\frac{dy}{dx} + 3y = e^{2x}$ | 7M | C02 | U |
| | b) | Solve: $(D^2 + 1)y = \tan x$ | 7M | C02 | Ap |
| 4 | a) | By changing the order of integration, evaluate $\int_0^1 \int_{e^x}^e \frac{dy dx}{\log y}$. | 7M | C03 | U |
| | b) | Using double integration, Find the area lying between the parabola $y = 4x - x^2$ and the straight line $y = x$. | 7M | C03 | AP |
| 5 | a) | Solve: $x^2 \frac{d^2y}{dx^2} - 4x \frac{dy}{dx} + 6y = x$ | 7M | C02 | U |
| | b) | Find the volume bounded by the coordinate planes, and the plane $\frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 1$. | 7M | C03 | Ap |
| 6 | a) | Find the directional derivative of $\phi = xy + yz + zx$ at $(1,1,1)$ in the direction towards the point $(2,-1,3)$. | 7M | C04 | Ap |
| | b) | Show that $\text{Curl grad } \phi = 0$ where ϕ is a scalar point function. | 7M | C04 | U |

- 7 a) A fluid motion is given by $\vec{f} = (y + z)\mathbf{i} + (x + z)\mathbf{j} + (y + x)\mathbf{k}$. Is this motion irrotational? If so find the scalar potential. 7M C04 Ap
- b) Prove that the area bounded by the closed curve C is $\frac{1}{2} \oint_C xdy - ydx$. 7M C05 U
- 8 a) Find the work done in moving a particle in the force field $\vec{F} = 3xy\mathbf{i} - 5z\mathbf{j} + 10x\mathbf{k}$ along the curve $x = t^2 + 1, y = 2t^2, z = t^3$ from $t = 1$ to $t = 2$. 7M C05 Ap
- b) Evaluate $\int_S \vec{F} \cdot \hat{n} ds$ where $\vec{F} = yz\mathbf{i} + xz\mathbf{j} + xy\mathbf{k}$ and S is the portion of the sphere $x^2 + y^2 + z^2 = 1$ which is in the first octant. 7M C05 R

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