



MARRI LAXMAN REDDY INSTITUTE OF TECHNOLOGY AND MANAGEMENT

(AN AUTONOMOUS INSTITUTION)

(Approved by AICTE, New Delhi & Affiliated to JNTUH, Hyderabad)

Accredited by NBA and NAAC with 'A' Grade & Recognized Under Section 2(f) & 12(B) of the UGC act, 1956

I B.Tech II Sem Supply End Examination, May 2022

Mathematics -II

(Common to all branches)

Time: 3 Hours.**Max. Marks: 70**

Note: 1. Question paper consists: Part-A and Part-B.

2. In Part - A, answer all questions which carries 20 marks.

3. In Part - B, answer any one question from each unit.

Each question carries 10 marks and may have a, b as sub questions.

PART- A**(10*2 Marks = 20 Marks)**

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|-------|---|----|-----|-----|
| 1. a) | Solve: $xdy + ydx = 0$. | 2M | CO1 | BL3 |
| b) | State the necessary condition for the differential equation $Mdx + Ndy$ to be exact. | 2M | CO1 | BL1 |
| c) | Find the particular solution of $(D^2 + D + 6)y = 0$. | 2M | CO2 | BL3 |
| d) | Solve: $(D^2 - 5D + 6)y = 0$. | 2M | CO2 | BL3 |
| e) | Define volume integral. | 2M | CO3 | BL1 |
| f) | Evaluate $\int_0^{11} \int_0^y y^2 dy dx$. | 2M | CO3 | BL5 |
| g) | Define curl of a vector field. | 2M | CO4 | BL1 |
| h) | If $\vec{r} = xi + yj + zk$ then find $\text{div } \vec{r}$. | 2M | CO4 | BL3 |
| i) | If S is any closed surface enclosing a volume V and $F = axi + byj + czk$, then find curl F. | 2M | CO5 | BL3 |
| j) | Define greens theorem. | 2M | CO5 | BL1 |

PART- B**(10*5 Marks = 50 Marks)**

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|-----------|--|-----|-----|-----|
| 2 | Solve the differential equation $\frac{dy}{dx} + \frac{2}{x}y = x^2y^2$. | 10M | CO1 | BL3 |
| OR | | | | |
| 3 | A body originally at $80^\circ C$ cools down to $60^\circ C$ in 20 minutes, the temperature of the air being $40^\circ C$. What will be the temperature of the body after 40 minutes from the original? | 10M | CO1 | BL3 |
| 4 | Solve: $\frac{d^2y}{dx^2} + 4\frac{dy}{dx} + 3y = e^{2x}$ | 10M | CO2 | BL3 |
| OR | | | | |
| 5 | Solve $(D^2 - 4D + 4)y = e^{2x} + 3$. | 10M | CO2 | BL3 |

- 6 Using double integration, Find the area lying between the parabola $y = 4x - x^2$ and the straight line $y = x$. 10M C03 BL3
- OR**
- 7 Solve: $x^2 \frac{d^2y}{dx^2} - 4x \frac{dy}{dx} + 6y = x$ 10M C03 BL3
- 8 Find the directional derivative of $\phi = xy + yz + zx$ at $(1,1,1)$ in the direction towards the point $(2,-1,3)$. 10M C04 BL3
- OR**
- 9 A fluid motion is given by $\vec{f} = (6xy + z^3)i + (3x^2 - z)j + (3xz^2 - y)k$. Is this motion irrotational? If so find the scalar potential. 10M C04 BL3
- 10 Evaluate $\int_S \vec{F} \cdot \hat{n} ds$ where $\vec{F} = yzi + xzj + xyk$ and S is the portion of the sphere $x^2 + y^2 + z^2 = 1$ which is in the first octant. 10M C05 BL3
- OR**
- 11 Verify Gauss Divergence theorem for $\vec{f} = (x^3 - yz)i - 2x^2yj + zk$ taken over the surface of the cube bounded by the planes $x=y=z=a$ and coordinate planes. 10M C05 BL3

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