



MARRI LAXMAN REDDY

INSTITUTE OF TECHNOLOGY AND MANAGEMENT

(AN AUTONOMOUS INSTITUTION)

(Approved by AICTE, New Delhi & Affiliated to JNTUH, Hyderabad)

Accredited by NBA and NAAC with 'A' Grade & Recognized Under Section 2(f) & 12(B) of the UGC act, 1956

II B.Tech I Sem Regular End Examination, March 2021

PROBABILITY THEORY AND STOCHASTIC PROCESSES

(ECE)

Time: 3 Hours.

Max. Marks: 70

Note: 1. Answer any FIVE questions.

2. Each question carries 14 marks and may have a, b as sub questions.

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|---|-----|--|----|----|----|
| 1 | a) | Obtain the expression for conditional density function and write its properties. | 7M | CO | BL |
| | b) | A company sells high fidelity amplifiers capable of generating 10W, 25W and 50W of audio power. It has on hand 100 of the 10W units, of which 15% are defective, 70 of the 25W units with 10% defective, and 30 of the 50W units with 10% defective. | 7M | CO | BL |
| | i) | What is the probability that an amplifier unit sold from the 10W units is defective? | | | |
| | ii) | If each wattage amplifier sells with equal likelihood, what is the probability of a randomly selected unit being 50W and defective? | | | |
| 2 | a) | A game of dice can be won outright if the sum of the two numbers showing up is either 7 or 11 when two dice are thrown. Represent the sample space and find the probability of winning outright. | 7M | CO | BL |
| | b) | Define CDF and write the properties of CDF of a random variable X. | 7M | CO | BL |
| 3 | a) | Find the mean of a random variable with Poisson distribution. | 7M | CO | BL |
| | b) | Define characteristic function of a random variable and show how moments can be generating using it. | 7M | CO | BL |
| 4 | a) | Classify random processes and explain. | 7M | CO | BL |
| | b) | Assume an ergodic random process X(t) has an autocorrelation function | 7M | CO | BL |

$$R_{XX}(\tau) = 18 + \frac{2}{6 + \tau^2} [1 + 4 \cos(12\tau)]$$

Find mean of X(t) and average power in X(t)

Key prepared by

Dr. Srinivas Bachu

Sey
12/3/21

- 5 a) The random variables Y_1, Y_2, X_1, X_2 are related by the relations shown below: $Y_1 = aX_1 + bX_2, Y_2 = cX_1 + dX_2$. Find $f_{Y_1Y_2}(y_1, y_2)$ in terms of joint density of X_1 and X_2 . 7M CO BL
- b) Explain the terms first order stationary process, WSS process and Strict sense stationary process with relevant expressions. 7M CO BL
- 6 a) Derive the expression for cross power density spectrum of random processes $X(t)$ and $Y(t)$. 10M CO BL
- b) Write the properties of power spectral density. 4M CO BL
- 7 a) If $X(t)$ is a stationary process, find the power spectrum of $Y(t) = A + BX(t)$ in terms of power spectrum of $X(t)$. Given A and B are constants. 7M CO BL
- b) A source emits different symbols a, b, c, d, e with respective probabilities $0.1, 0.2, 0.1, 0.1, 0.5$. Obtain the code words using Huffman coding and also calculate entropy. 7M CO BL
- 8 a) State Shannon-Hartley law and explain its significance. Also derive Shannon's limit. 7M CO BL
- b) Classify noise sources and write notes on thermal noise 7M CO BL

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