



II B.Tech II Sem Supply End Examination, March 2022  
**Laplace Transforms, Numerical Methods and Complex Variables**  
**(EEE & ECE)**

**Time: 3 Hours.****Max. Marks: 70**

Note: 1. Answer any FIVE questions.

2. Each question carries 14 marks and may have a, b as sub questions.

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|---|---|-----|-----|----|
| 1 | a) Find inverse Laplace transform of the function $\frac{1}{s^2(s+3)}$ .  | 7M  | C01 | BI |
|   | b) Evaluate $L\left\{\int_0^t e^{-t} \cos t dt\right\}$ .   | 7M  | C01 | BI |
| 2 | Using Laplace transform, solve $(D^2 + 1)x = t \cos 2t$ given $x = 0, \frac{dx}{dt} = 0$ at $t = 0$ .   | 14M | C01 | BI |
| 3 | a) By using method false position, find the root of the equation $\cos x - xe^x = 0$ .  | 7M  | C02 | BI |
|   | b) Given $\sin 45^\circ = 0.7071, \sin 50^\circ = 0.7660, \sin 55^\circ = 0.8192$ and $\sin 60^\circ = 0.8660$ . Find $\sin 52^\circ$ using Newton's interpolation formula. | 7M  | C02 | BI |
| 4 | a) Show $\Delta^2 x^{(m)} = m(m-1)x^{(m-2)}$ , $m$ is a positive integer and $h = 1$ .  | 7M  | C02 | BI |
|   | b) Evaluate the integral $\int_0^1 \frac{dx}{3+2x}$ using trapezoidal rule.   | 7M  | C03 | BI |
| 5 | Use Runge-Kutta method of order four to find $y$ when $x = 0.6$ given that $\frac{dy}{dx} = 1 + y^2, y(0) = 0$ .  | 14M | C03 | BI |
| 6 | a) Find the conjugate harmonic function of the harmonic function $U = x^2 - y^2 - x$ .  | 7M  | C04 | BI |
|   | b) Show that $xy^2$ cannot be real part of an analytic function   | 7M  | C04 | BI |
| 7 | a) Find the general value of $\log(1 + i)$  | 7M  | C04 | BI |
|   | b) Evaluate $\int_c \frac{z \sec z}{(1-z^2)} dz$ where $c$ is the ellipse $4x^2 + 9y^2 = 9$ .   | 7M  | C05 | BI |
| 8 | a) Find Laurent expansion of $\frac{1}{z^2 - 4z + 3}$ for $1 <  z  < 3$ .   | 7M  | C05 | BI |
|   | b) Find the residue of $1/(z-1)(z-2)$ .   | 7M  | C05 | BI |