



II B.Tech I Sem Supply End Examination, July-2022
Laplace Transforms Series Solutions and Complex Variables
 (EEE & ECE)

Max. Marks: 70

- Note: 1. Question paper consists: Part-A and Part-B.
 2. In Part - A, answer all questions which carries 20 marks.
 3. In Part - B, answer any one question from each unit.
 Each question carries 10 marks and may have a, b as sub questions.

PART- A

(10*2 Marks = 20 Marks)

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|-------|--|----|-----|---|
| 1. a) | Find the Laplace transform of unit step function | 2M | CO1 | U |
| b) | State the conditions for the existence of a Laplace Transform | 2M | CO1 | R |
| c) | State Dirichlet's conditions for Fourier series | 2M | CO2 | R |
| d) | Explain briefly about Half range cosine series expansion of a function | 2M | CO2 | U |
| e) | Define ordinary point and singular point of a Differential Equation | 2M | CO3 | R |
| f) | Write Bessel's Differential equation of order n. | 2M | CO3 | U |
| g) | Write Cauchy Riemann equations in Cartesian coordinates. | 2M | CO4 | U |
| h) | Define Analytic function. | 2M | CO4 | R |
| i) | State Cauchy integral theorem | 2M | CO5 | R |
| j) | Find the residue of $f(z) = \frac{z^2}{(z-1)(z-2)^2}$ at $z=2$. | 2M | CO5 | U |

PART- B

(10*5 Marks = 50 Marks)

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|-----------|----|---|-----|-----|----|
| 2 | a) | Using Laplace Transforms evaluate the integral $\int_0^{\infty} te^{-3t} \sin t dt$ | 5M | CO1 | AP |
| | b) | Find Laplace transform of $f(t) = e^{-3t} (2 \cos 5t - 3 \sin 5t)$ | 5M | CO1 | U |
| OR | | | | | |
| 3 | | Using Laplace transform method, Solve $\frac{d^2x}{dt^2} + 3\frac{dx}{dt} + 2x = e^{-t}$, given that $x(0)=0, x'(0) = 1$. | 10M | CO1 | AN |
| 4 | a) | Find Fourier series of the function $f(x) = x^2$ on $0 < x < 4$. | 5M | CO2 | U |
| | b) | Find the Half range Cosine series of $f(x) = (x-1)^2$ in $0 < x < 1$. | 5M | CO2 | AP |

OR

5 Find the Fourier series expansion of $f(x) = \begin{cases} -\pi, & -\pi < x < 0 \\ 0, & 0 < x < \pi \end{cases}$ 10M C02 AN

6 a) Prove that $J_n(x) = \frac{x}{2n} [J_{n-1}(x) + J_{n+1}(x)]$ 5M C03 U

b) Prove that $J_{\frac{1}{2}}(x) = \sqrt{\frac{2}{\pi x}} (\sin x)$ 5M C03 AP

OR

7 Explain briefly about Orthogonality of Bessel functions. 10M C03 AN

8 a) Discuss the analyticity of $f(z) = Z^2$ 5M C04 U

b) Determine the Analytic function $f(z)$ whose real part is $e^{2x}(x \cos 2y - y \sin 2y)$. 5M C04 AP

OR

9 Show that the function $f(z) = \frac{x^3(1+i) - y^3(1-i)}{x^2 + y^2}$ ($z \neq 0$), $f(z)=0$, $z=0$ 10M C04 AN

is continuous and Cauchy Riemann equations are satisfied at the origin, yet $f'(0)$ does not exist.

10 a) Using Cauchy integral formula evaluate the integral $\oint_c \frac{e^z}{\left(z - \frac{\pi}{6}\right)^3} dz$, 5M C05 U

where $c: |z|=1$

b) Apply Residue theorem to evaluate the integral $\oint_c \frac{1-2z}{z(z-1)(z-2)} dz$, 5M C05 AP

where $c: |z|=1.5$.

OR

11 Find the Laurent's series expansion of $f(z) = \frac{z}{(z-1)(z-3)}$ in the 10M C05 AN

region (i) $|z| < 1$ (ii) $1 < |z| < 3$ (iii) $|z| > 3$

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