



# MARRI LAXMAN REDDY INSTITUTE OF TECHNOLOGY AND MANAGEMENT

(AN AUTONOMOUS INSTITUTION)

(Approved by AICTE, New Delhi &amp; Affiliated to JNTUH, Hyderabad)

Accredited by NBA and NAAC with 'A' Grade &amp; Recognized Under Section 2(f) &amp; 12(B) of the UGC act, 1956

II B.Tech II Sem Regular End Examination, July 2022

## Discrete Mathematics (CSE/IT/CSI/CSC/CSD)

Time: 3 Hours.

Max. Marks: 70

Note: 1. Question paper consists: Part-A and Part-B.

2. In Part - A, answer all questions which carries 20 marks.

3. In Part - B, answer any one question from each unit.

Each question carries 10 marks and may have a, b as sub questions.

### PART- A

(10\*2 Marks = 20 Marks)

- |       |  |    |     |     |
|-------|--|----|-----|-----|
| 1. a) | Define well-formed formulae and clause form.   | 2M | C01 | BL1 |
| b)    | Write converse and inverse for the statement "If Sun rises in the east then $3*7=98$ "   | 2M | C01 | BL1 |
| c)    | Give suitable examples for a relation which is not equivalence relation  | 2M | C02 | BL1 |
| d)    | Let $X=\{1,2,3,4,5,6\}$ and R be a relation defined as $(x,y) \in R$ if and only if $x-y$ is divisible by 3. Find the elements of relation of R.         | 2M | C02 | BL3 |
| e)    | From 6 boys and 4 girls, 5 are to be selected for admission for a particular course. In How many ways can this be done if there must be exactly 2 girls? | 2M | C03 | BL3 |
| f)    | Calculate the number of binary numbers with 9 one's and 5 zero's   | 2M | C03 | BL3 |
| g)    | Write the characteristic equation for the following recurrence relation $a_n - 4a_{n-4} = 0, n \geq 4$ and solve it                                      | 2M | C04 | BL1 |
| h)    | What is homogeneous recurrence relation?   | 2M | C04 | BL1 |
| i)    | Define Bipartite graph and Isomorphic graphs.  | 2M | C05 | BL1 |
| j)    | Define spanning tree. What are its characteristics?  | 2M | C05 | BL1 |

### PART- B

(10\*5 Marks = 50 Marks)

- |       |  |    |     |     |
|-------|--|----|-----|-----|
| 2. a) | Obtain the PCNF and PDNF of $(P \rightarrow (Q \wedge R)) \wedge (\sim P \rightarrow (\sim Q \wedge \sim R))$ .  | 5M | C01 | BL3 |
| b)    | Verify the validity of the following arguments. "Every living thing is a plant or an animal. Logu's dog is alive and it is not a plant. All animals have heart. Therefore Logu's dog has a heart." | 5M | C01 | BL3 |

OR

- |    |  |     |     |     |
|----|--|-----|-----|-----|
| 3. | Without using truth tables prove that $((P \vee Q) \rightarrow (\neg P (\neg Q \vee \neg R))) \vee (\neg P \rightarrow Q) \vee (\neg Q \rightarrow R)$ is a tautology. | 10M | C01 | BL3 |
|----|--|-----|-----|-----|

- 4 a) Explain properties of binary relations with examples 5M C02 BL4  
 b) Draw the Hasse diagram for the partial ordering  $\{(A, B): A \leq B\}$  on the power set  $e(S)$  where  $S=\{a, b, c\}$  and  $\leq$  is subset relation. 5M C02 BL1
- OR**
- 5 In a lattice  $(L, \leq, \wedge, \vee)$  state and prove the laws idempotent, commutative, association and absorption. 10M C02 BL3
- 6 a) Show that given any 52 integers, there exists two of them whose sum or else whose difference is divisible by 100 5M C03 BL3  
 b) State and prove multinomial theorem. 5M C03 BL3
- OR**
- 7 State and prove extended pigeon principle. Using it show that 9 colors are used to paint 100 houses at least 12 houses will be of the same color. 10M C03 BL3
- 8 a) Find the recurrence relation and initial condition for the following sequence: 6, -18, 54, -162 ... 5M C04 BL3  
 b) Define generating function. Write the sequence generated by the  $2x^2(1-2x)^{-1}$  5M C04 BL3
- OR**
- 9 Find the solution for the Fibonacci series  $a_n = a_{n-1} + a_{n-2}$ ,  $n > 2$  and  $a_0 = 1, a_1 = 1$ . 10M C04 BL3
- 10 a) Show that a simple complete digraph with  $n$  nodes has the maximum number of edges  $n(n-1)$ . Assuming that there are no loops 5M C05 BL3  
 b) State and explain graph coloring problem. Give its applications 5M C05 BL4
- OR**
- 11 Explain Kruskal's algorithm with example. 10M C05 BL4